# ELEMENTARY MATH MASTERY EDITION

Dr Rhonda Farkota

mathmasteryseries.com.au



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# **MATH MASTERY SERIES**

#### **Direct Instruction**

Direct Instruction (DI) is a teaching model created by Professor Siegfried Engelmann and the University of Oregon. Based on the premise that clear, unambiguous teaching, enhances student learning, DI lessons are meticulously scripted, in clear, unambiguous language, with each lesson structured in small incremental portions.

#### **Farkota Direct Instruction model**

Adapting the scripted lesson concept, the Farkota Direct Instruction (FDI) model modernises the delivery process, and streamlines the script in a manner that strikes a balance between teacher-directed learning and student-directed learning.

#### **FDI Math Mastery Series**

The Math Mastery Series (MMS) programs (JEMM, JEMM+ and EMM) consist of daily scripted lessons composed of strands each starting at base level where foundations are laid. They serve as daily diagnostic tools incorporating assessment as an integral part of the learning process. Student responses, coupled with their own analysis of any incorrect response given during a lesson, provide teachers with reliable diagnostic information better than any that can be acquired in a formal test situation. This is crucial in that it allows teacher feedback to specifically target individual student misunderstanding.

Maximising every benefit a mental math program is capable of yielding MMS programs:

- map student progress
- identify precisely where and when students experience difficulty
- contain inbuilt assessment and correction procedures
- instil fluency and automaticity in fundamental math skills.

## THE MATH MASTERY SERIES PROGRAMS

# Elementary

## Math Mastery

Ideally suited to upper primary and first year secondary students, and secondary school remedial classes.

Requires daily 15–20 minutes to implement, plus 5–10 minutes for corrections and feedback.

EMM features 160 lessons, each composed of 20 strands. Students answer one question per strand daily:

- Addition
- Subtraction
- Multiplication
- Division
- Number patterns
- Equations and inverse operations
- Whole number properties
- Fractions
- Decimals
- Measurement
- Space
- Geometry
- Average, percentage, ratio, chance
- Math language
- Money
- Time
- Algebra
- Visual perception
- Data analysis
- Problem solving

These programs help all students, but particularly those who:

- · Have not reached required numeracy level for their age
- Have low motivation to learn, or low self-efficacy
- Are classified as at-risk learners
- Have difficulty concentrating, and would benefit from repeated structured teaching and practice.

#### **MMSanimation**

**MMS**animation is a voice-over with animation of each lesson, for each program. These **animations reflect** that critical part of the Lesson **script** (shown in coloured CAPS) **that requires the teacher to point on the electronic display. MMS**animation was created primarily for three reasons: firstly, absent students need to catch up; secondly, support for students with special needs; and thirdly, general teacher support. **EMM**animation: see **mathmasteryseries.com.au/mmsanimation** 

# JEMM-

Math Mastery+

Ideally suited to middle primary and upper primary students, and first year secondary school remedial classes.

Requires daily 15–20 minutes to implement, plus 5–10 minutes for corrections and feedback.

JEMM+ features 120 lessons, each composed of 15 strands. Students answer one question per strand daily:

- Counting
- Addition
- Subtraction
- Multiplication
- Division
- Number patterns
- Fractions
- Decimals
- Measurement
- Space
- Data and Chance
- Money
- Time
- Visual perception
- Problem solving

# JEMM

Junior Elementary Math Mastery

Ideally suited to middle primary students, and primary school remedial classes.

Requires daily 10–15 minutes to implement, plus 3–7 minutes for corrections and feedback.

JEMM features 80 lessons. Students answer one question per strand daily with Lesson 1 introducing:

- Whole number addition
- Whole number subtraction
- Number facts
- Place value
- Number patterns

Building on these base strands the following lessons introduce:

- Lesson 21 Money
- Lesson 31 Measurement
- Lesson 41 Fractions
- Lesson 51 Time
- Lesson 61 Data and Chance

# **Contents**

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## **EMM INTRODUCTORY NOTES**

Generally speaking, mental math programs are warm-up exercises consisting of a 'grab-bag' of questions taken from various math strands with little constructive thought behind the design. Of limited value as learning programs, they do however perform one important function: the oral presentation and constraint on time pressures students to concentrate. Unfortunately, teachers are encouraged to, and often *do*, use them as work-sheets, thus failing to capitalise on the important contribution aural perception and pressure of time can play in the learning process. Although there has been a general failure to exploit the enormous developmental potential mental math programs are capable of yielding, the MMS is purpose-built to maximise this potential. Specifically designed around the document: Mathematics – a curriculum profile for Australian schools, EMM is a daily program for the entire class that can be easily integrated into any school's math curriculum for upper primary, first year secondary and remedial classes.

EMM comprises **20 different strands** (one question from each strand per lesson). It requires **15–20 minutes to implement, plus 5–10 minutes for instant feedback, diagnosis and correction procedures**. Diligent implementation over the course of the school year will see students answering a total of 3600 questions (presented orally) at the end of which time they will have achieved mastery (equated here with an average daily score of at least 80%) of fundamental math skills in all core areas.

Each of the EMM 20 strands **starts at base level** and moves through its particular field, merging and interrelating with the 19 other strands being run concurrently. Since the **daily incremental portions learned by the students in each strand are small**, and because they are **reinforced and built upon** in subsequent lessons, **they are mastered**.

EMM comes in a **teacher-friendly format** with **all lesson scripts provided; those with little math expertise will find it easy to implement**. Each lesson is complete within itself, and each strand has been choreographed with the focus on overall mastery of basic math skills. The teacher simply presents the program in the scripted format. The EMM electronic reference stimuli (ERS) includes all diagrams, formulas and display material, maximising time efficiency and allowing for effortless implementation. Should electronic delivery be unavailable, board presentations are perfectly adequate.

A perennial problem for teachers at the start of each school year is the diverse, and all too often, inadequate, academic standard of their new class. In an ideal world, teachers could safely assume that students entering their classroom on the first day of a school year would be capable of performing at a level appropriate to their particular grade, and that the foundations necessary for them to progress satisfactorily on their academic paths would be firmly in place. Unfortunately, this is seldom the case. A primary objective of EMM is to address this problem.

At the outset, EMM assumes nothing in terms of student academic level. The program has been **designed to accommodate every student, and elevate every student's academic level no matter where they start from**, provided, of course, the students do not have significant learning disabilities. In the early stages of EMM the questions are basic. Students with developed skills may wonder what the program has to offer. This will not last long. These basic questions quickly build to questions that will challenge every student. Of course, the challenge to some will be greater than others, but every student will have been taught the skills necessary to answer every question—there are no tricks.

The design of EMM is such that **students discover for themselves the formulas necessary to solve relatively complex problems automatically and speedily**. Students soon see they are up to the task, and because they know they have acquired the necessary skills, actually look forward to the challenge. Once foundations to the core areas have been laid and tested, they are built on with small precise portions. None of this incremental information is left on the shelf. Students move on to questions that gradually increase in complexity, all the while relying on the skills they have acquired along the way. These **questions shift from abstract numbers to real-life situations** so students see the relative worth of mathematics in situations that arise in the everyday world. Students quickly learn that everything they are taught is important; everything they learn is revisited, developed further, and gradually integrated into the broad mathematical landscape. This **gradual and consistent development of skills** is one of the key elements in the success of the Math Mastery Series.

The traditional practice of teaching mathematics in single topics creates many problems for students. Presenting them with a heap of new information in one hit, expecting them to master it; then move onto another, often unrelated topic, master that too, and so on, is a big ask. The problem is compounded when students are not re-familiarised with the topics throughout the year. EMM circumvents this problem by running 20 concurrent strands. Because the strands are run concurrently, **students are soon familiar with the many connections existing between the various math disciplines, and become fluent and automatic in applying them**.

An essential feature of EMM is its **ability to focus student attention** on the learning process. This is achieved by the teacher orally introducing the concepts and questions at a pace easily enough accommodated by students who are concentrating, but which gives them no time to tune-out. Students stay alert because they know a question immediately follows the introduction of a concept. The **electronic reference stimuli (ERS)** further **enhances student engagement** and, in particular, **helps students with special needs** stay on track.

It is important to note that there should be no interruption to the lesson once in progress. The stream of student focus and concentration must be on what the teacher is saying. This is best achieved by conducting the lesson at a relatively brisk pace, and not stopping for queries or distracted students who want the question repeated more than once (all questions are put to the students twice). Queries should be attended to after correction time in *What bugs you*? Students who are used to working at a slower pace quickly learn what's required of them.

In maximising the benefits of EMM the importance of the teacher's role cannot be over-emphasised. Because the program's lessons are interdependent, and because the interrelating strands build entirely upon themselves, diligent teacher implementation is essential.

1 Addition	11 Space
2 Subtraction	12 Geometry
3 Multiplication	13 Average, percentage, ratio, chance
4 Division	14 Math language
5 Number patterns	15 Money
6 Equations and inverse operations	16 Time
7 Whole number properties	17 Algebra
8 Fractions	18 Visual perception
9 Decimals	19 Data analysis
10 Measurement	20 Problem solving

## **THE EMM STRANDS**

V

## **USING THE SCRIPT**

EMM provides teacher alternate modes of delivery.

Electronic Reference Stimuli (ERS) includes all visual diagrams, formulas and display material AND

Colour Masters for use where electronic delivery unavailable.

Both modes have been incorporated into the script.

Note: ERS download information is provided by email at time of purchase. For queries contact **hello@mathmasteryseries.com.au**.



## **PROGRAM STRUCTURE**

EMM consists of 160 scripted lessons structured in rounds of five. Whenever a new concept is introduced it will always be in the first lesson of a round. It is in the last lessons of the rounds where these concepts will be put to the test.

	Number of sessions to complete MMS			
	ЕММ	JEMM+	JEMM	TOTAL
Teacher delivered scripted lessons	160	120	80	360
Student Self-evaluations	8	6	4	18
Marathons	40	30	20	90
EMM/JEMM+/JEMMathon tasks	8	6	4	18
Round tasks	24	18	12	54
Challenges	4	4	4	12
TOTAL number of sessions required	244	184	124	552

## **EMM SESSION SCHEDULE**

SESSION	NUMBER

		Daily Data Round 01 L01-05	01, 02, 03, 04, 05
I		Round 01 Task	06
l		Daily Data Round 02 L06–10	07, 08, 09, 10, 11
	1	Round 02 Task	12
l	S	Daily Data Round 03 L11-15	13, 14, 15, 16, 17
l	N	Round 03 Task	18
	30L	Daily Data Round 04 L16–20	19, 20, 21, 22, 23
		Self-evaluation L01-20	24
		EMMathon 1	25, 26, 27, 28, 29
		EMMathon 1 TASK	30

#### SESSION NUMBER

Daily Data Round 05 L21–25	31, 32, 33, 34, 35
Round 05 Task	36
Daily Data Round 06 L26-30	37, 38, 39, 40, 41
Round 06 Task	42
Daily Data Round 07 L31-35	43, 44, 45, 46, 47
Round 07 Task	48
Daily Data Round 08 L36-40	49, 50, 51, 52, 53
Self-evaluation L21-40	54
EMMathon 2	55, 56, 57, 58, 59
EMMathon 2 TASK	60
	Daily Data Round 05 L21-25 Round 05 Task Daily Data Round 06 L26-30 Round 06 Task Daily Data Round 07 L31-35 Round 07 Task Daily Data Round 08 L36-40 Self-evaluation L21-40 EMMathon 2 EMMathon 2 TASK

#### SESSION NUMBER

	Daily Data Round 09 L41-45	61, 62, 63, 64, 65
	Round 09 Task	66
N	Daily Data Round 10 L46-50	67, 68, 69, 70, 71
T	Round 10 Task	72
S	Daily Data Round 11 L51-55	73, 74, 75, 76, 77
Z	Round 11 Task	78
NO	Daily Data Round 12 L56-60	79, 80, 81, 82, 83
Ĕ	Self-evaluation L41-60	84
	EMMathon 3	85, 86, 87, 88, 89
	EMMathon 3 TASK	90

#### SESSION NUMBER

	OLOGION	NOMBEN
	Daily Data Round 13 L61-65	91, 92, 93, 94, 95
	Round 13 Task	96
o	Daily Data Round 14 L66-70	97, 98, 99, 100, 101
9.1	Round 14 Task	102
S +	Daily Data Round 15 L71–75	103, 104, 105, 106, 107
Ő	Round 15 Task	108
Inc	Daily Data Round 16 L76-80	109, 110, 111, 112, 113
ŭ	Self-evaluation L61-80	114
	EMMathon 4	115, 116, 117, 118, 119
	EMMathon 4 TASK	120

#### SESSION NUMBER

	Daily Data Round 17 L81-85	121, 122, 123, 124, 125
	Round 17 Task	126
0	Daily Data Round 18 L86-90	127, 128, 129, 130, 131
7-2	Round 18 Task	132
s 1	Daily Data Round 19 L91–95	133, 134, 135, 136, 137
Q	Round 19 Task	138
O	Daily Data Round 20 L96–100	139, 140, 141, 142, 143
č	Self-evaluation L81–100	144
	EMMathon 5	145, 146, 147, 148, 149
	EMMathon 5 TASK	150

#### SESSION NUMBER

Daily Data Round 21 L101–105	151, 152, 153, 154, 155
Round 21 Task	156
Daily Data Round 22 L106-110	157, 158, 159, 160, 161
Round 22 Task	162
Daily Data Round 23 L111–115	163, 164, 165, 166, 167
Round 23 Task	168
Daily Data Round 24 L116–120	169, 170, 171, 172, 173
Self-evaluation L101–120	174
EMMathon 6	175, 176, 177, 178, 179
EMMathon 6 TASK	180

**ROUNDS 21-24** 

ROUNDS 25-28

#### SESSION NUMBER

Daily Data Round 25 L121-125	181, 182, 183, 184, 185
Round 25 Task	186
Daily Data Round 26 L126–130	187, 188, 189, 190, 191
Round 26 Task	192
Daily Data Round 27 L131-135	193, 194, 195, 196, 197
Round 27 Task	198
Daily Data Round 28 L136-140	199, 200, 201, 202, 203
Self-evaluation L121-140	204
EMMathon 7	205, 206, 207, 208, 209
EMMathon 7 TASK	210

#### SESSION NUMBER

N	Daily Data Round 29 L141–145	211, 212, 213, 214, 215
	Round 29 Task	216
	Daily Data Round 30 L146–150	217, 218, 219, 220, 221
i D	Round 30 Task	222
	Daily Data Round 31 L151–155	223, 224, 225, 226, 227
	Round 31 Task	228
	Daily Data Round 32 L156–160	229, 230, 231, 232, 233
	Self-evaluation L141-160	234
	EMMathon 8	235, 236, 237, 238, 239
	EMMathon 8 TASK	240

SESSION	NUMBER
CHALLENGE 1	241
CHALLENGE 2	242
CHALLENGE 3	243
CHALLENGE 4	244

## myEMMdata Student Workbook

The EMM Student Workbook flows with the EMM program, maximising time-efficiency and bestowing distinct advantages from both educational and practicality viewpoints. Delivering a particularly strong educational component, the workbook slots in perfectly with the *Australian Curriculum Sub-strand, Data Representation and Interpretation*. Students record, summarise and represent their own personal data daily, thereby enhancing their engagement with the learning process in the most positive way. Student employment of various forms of data representation enables them to map their performance, while also serving as a subtle, yet powerful, learning adjunct.

To effectively diagnose and remediate, the teacher and student do the hard yards together. In order to accurately diagnose student knowledge and understanding, the teacher must drill down, or up, and this is best achieved by incorporating diagnostic assessment into daily teaching. The MMS Workbook has been deliberately designed so that teachers can check the students' responses to specifically target misunderstanding and monitor progress.

#### Workbook components:

**Daily Data:** Each day, students record and summarise their own data. For incorrect responses, classified as Bugs, students shade the BugKey in the corresponding row on the BugBoard. This allows teachers to continually monitor progress and determine whether remediation is needed. For example, see myEMMdata pages 2–9.

**Visual representation:** This provides foundational knowledge and daily practice in reading and interpreting data to prepare students for the *Round task*. For example, see myEMMdata pages 2–9.

**Round task:** EMM is structured into 32 rounds each consisting of 5 lessons. At the end of each round students read, interpret and complete tables and graphs building on the *Visual representation* foundational knowledge. For example, see myEMMdata pages 10–11.

**Self-evaluation:** After every 4 rounds (20 lessons) students self-evaluate and reflect on their growth in knowledge, understanding and achievement. They record their feelings, providing teachers with an insight into their thoughts, and the opportunity to comment. (Thanks to Kevin Duffy, Principal WA, for his valuable input here.) For example, see myEMMdata pages 12–13.

**EMMathon:** These restructured lessons enable students to demonstrate their BugFree status. EMMathons affirm fluency, further enhance self-efficacy, and assess how well students have consolidated their knowledge and understanding. For example, see myEMMdata pages 14–15.

**EMMathon to BugFree:** Students convert their scores to percentages to determine their BugFree status. This encourages students to concentrate on personal growth rather than comparison with other students. Conversions should be performed either after each EMMathon, or after each Marathon. See myEMMdata pages 58–61; 118–121.

**Challenge:** These are designed to stimulate the thinking process, requiring students to reflect on what they have learned. Ideally, they are implemented at the end of the EMM program. See myEMMdata pages 122–125.

**Awards:** These motivate and reward students by emphasising growth, effort and completion of tasks. Club BugFree Award: For students who score all correct responses over a number of consecutive lessons. The recommended benchmark for this award is 20 consecutive lessons. Sixteen awards are provided allowing teachers to lower the benchmark at their discretion. See myEMMdata pages 127–133. Optional awards (Accurate Marking Award, Neat Workbook Award) could also be assessed in 20 lesson blocks. See myEMMdata pages 135–141.

## PRETEST

Before beginning the program, Lesson 80 and/or Lesson 160 may be used as a pretest. Once Lesson 80 has been completed the results can be compared to the pretest. (Thanks to Far North Queensland Region, Education Queensland, for this suggestion.)

## INTRODUCTORY SCRIPT FOR IMPLEMENTING MMS WITH myEMMdata Student Workbook

- 1. Write on board: Lesson 1 and today's date.
- 2. SAY: Open your Workbook to page 3 and find Lesson 1. You are going to write your answers to Lesson 1 in this column. Write the **DATE** above Lesson 1.
- 3. SAY: Now look at page 2 and find the Lesson 1 Workspace. Use this space for working out what you cannot do in your head.
- 4. Follow the Elementary Math Mastery Lesson 1 script pages 2–5 up to the corrections.
- 5. SAY: Over the coming lessons I may decide to make an award for accurate marking.
- 6. Correct all questions, see EMM page xi.
- 7. After corrections and before debugging SAY: Look at page 3 and find the word BugBoard. A Bug is an incorrect response where you are unable to understand why you are wrong. Look at the BugBoard. For those incorrect responses classified as Bugs shade the BugKey on the corresponding row under the column headed one.
- 8. DEBUG see EMM page xi.
- 9. After debugging SAY: Look at page 2 and find the arrow at the bottom of the page. The arrow is pointing to the Visual representation images. I'll read what it says. You follow: For each Lesson the whole of my data is represented in a bar made of 20 rectangles. From the baseline, I summarise my data by shading the number of rectangles equal to my score. You can see the bar under Lesson 1. From the baseline, shade the number of rectangles equal to your score.
- 10. Observe and check students have followed correctly.

**Note:** At the end of Lesson 5, introduce the first Round task. Ideally, a Round task requires an entire session and should be completed before commencing the next lesson.

SAY: Look at page 3 and find the arrow at the bottom of the page. The arrow is pointing forward. I'll read what it says. You follow: After recording and summarising my data for these 5 lessons, I go to page 10 and complete my Task for this Round. Everyone turn to page 10 and complete the Round 1 Task.

#### myEMMdata Student Workbook Electronic Display Material

To support your introduction go to the Math Mastery Series website under Resources: **mathmasteryseries.com.au/student-workbook**.

## **EMMATHON**

After students have self-evaluated their first group of 20 lessons (myEMMdata page 12), teachers are advised to run an EMMathon.

An EMMathon is made up of 5 Marathons. A Marathon consists of 2 lessons from the previous 10, where the teacher presents the entire 40 questions without any teacher modeling (i.e. teacher presents the question only).

The first Marathon (myEMMdata page 14, coded M01 in the plan below) revisits Lessons 11 and 12 (coded L11–L12) where only the question is presented. The second Marathon (M02) revisits Lessons 13 and 14 (L13–L14) etc. After the first EMMathon is completed, teachers return to the program presenting Lessons 21–40 as per the EMM script.

After students have self-evaluated their second group of 20 lessons (myEMMdata page 26), teachers run a second EMMathon (myEMMdata page 28), then return to the program, and so on. Each of the darker shaded sections below denote an EMMathon round. An EMMathon round consists of 10 lessons restructured into 5, effectively adding 40 sessions to the EMM program.



Teachers may consider commencing EMMathons later in the program or adapting them in some other way that better befits the ability of their students. For example, a Marathon could consist of a set of 4 lessons from the previous 20. See pages 146–149 myEMMdata Student Workbook for optional template.

Electronic Reference Stimuli: EMMathon – see ERS provided by email at time of purchase. For queries contact **hello@mathmasteryseries.com.au**.

## **EMMathon to BUGFREE**

EMMathons provide students with the opportunity to demonstrate they are BugFree; they affirm fluency and further enhance self-efficacy. Following the first EMMathon students should complete EMMathon 1 Task, myEMMdata page 58, and then, go to page 60 and convert their own EMMathon 1 scores to BugFree levels. Conversions should be performed after each EMMathon.

## **CORRECTIONS**

It is important to be consistent with corrections.

The following is a suggested plan:

- Students exchange books for corrections
- · Teacher selects students to answer from the work they are correcting
- Teacher announces the question number and the selected student calls the answer
- Teacher repeats the given answer indicating correct if incorrect teacher selects another student to respond, and so on
- Students circle any incorrect response if correct no mark recorded.

To gauge instant feedback on the overall class performance, have students raise hands each time they mark an incorrect response.

After marking:

- Books are returned and students record their total number of correct responses at the bottom of the column for that lesson
- Students shade incorrect responses classified as Bugs (see below) in the corresponding row on the BugBoard (see page xv).

At a glance the teacher can now gauge the overall performance of each student, for each strand, for each round. Students who score all correct responses over 20 consecutive lessons receive a Club Bugfree Award. The teacher may lower the benchmark at his/her discretion.

### **WHAT BUGS YOU?**

A BUG is an incorrect response where the student is unable to understand why he or she is wrong. It is important to DEBUG directly after corrections. Select students to identify questions that are causing them concern (What bugs you?). Revisiting the script with class discussion may be required here. This debugging process is the most critical step on the path to mastery. NOTE: Question 20 is designed to challenge students luring them into the process of constructive thinking. It is therefore recommended that this question not be debugged.

## LOW-PERFORMING STUDENT SUPPORT: CHIN-IT APPROACH

The MMS was designed for single class grade groups, however, low-performing students may benefit from working in a group following the MMS CHIN-IT approach. In a nutshell, the CHIN-IT approach involves the teacher presenting each round twice (5 lessons make up a round). In the first presentation of the round, sections are presented lock-step with students writing each response on their individual whiteboards, and then they CHIN-IT (display whiteboard under chin); the teacher scans the responses and if no errors are evident, moves on to the next section etc, otherwise the teacher debugs errors. If after three attempts the question is not debugged the teacher moves to the next section, noting students who need individual attention. After the round has been completed, or after each lesson, the teacher repeats the round (or lesson), *as per normal* (i.e. presents entire lesson, corrects, and debugs the student-identified bugs recorded in their Student Workbook).

## **SUGGESTED IMPLEMENTATION PLAN:** Average ability Yr 3, 4, 5, 6 and 7

Programs at each year level must be commenced at Lesson 1, and must be completed, before moving on to the next program. The following plan illustrates the stages at which the JEMMathons, JEMM+athons, and EMMathons commence. For example, Year 6 students complete lessons 1–60 before doing their first EMMathon.

Note: Low-performing students would benefit from completing all JEMMathons, JEMM+athons, and EMMathons.

Y	ear 3	;													
JEMM L01–L20 JEMM L21–L40						JEN	JEMM L41-L60			JEM	JEMM L61-L80				
	M01	L01-L04	REE		M06	L21-L24	Ë		M11	L41-L44	끮		M16	L61-L64	Ш
E	M02	L05-L08	UGFI	io	M07	L25-L28	UGFI	ы	M12	L45-L48	E E	5	M17	L65-L68	19L
uatic	M03	L09-L12	to B	Iluat	M08	L29-L32	to B	uati	M13	L49-L52	to Bl	uati	M18	L69-L72	to Bl
eval	M04	L13-L16	UOL	-eva	M09	L33–L36	БС	eva	M14	L53–L56	not	eval	M19	L73–L76	nor
Self-	M05	L17-L20	Matl	Self	M10	L37-L40	Matl	Self-	M15	L57-L60	Math	Self-	M20	L77–L80	Math
	JEMMathon 1						JEMMathon 3 목				JEM	Mathon 4	JEM		

	I Gal ·	•																				
<b>JEMM+</b> L01–L20 <b>JEMM+</b> L21–L40		JEN	<b>JEMM+</b> L41-L60			JEMM+ L61-L80				JEMM+ L81-L100				JEN	IM+ L101-L120							
	M01	L11-L12	RE	Ν	106	L31–L32	REE		M11	L51–L52	끮			L71-L72	RE				REE			REE
2	5 M02	L13-L14	UGF	N	107	L33-L34	UGF	ioi	M12	L53-L54	UGF	ioi		L73-L74	SUGF	ю			SUGF	ion		SUGF
+ ci la	M03	L15-L16	to	∧ aluat	108	L35-L36	to E	aluat	M13	L55-L56	to E	aluat		L75-L76	to E	aluat		L95-L96	toE	aluat		to E
2000	M04	L17-L18	thon	N-eve	109	L37-L38	thon	-eva	M14	L57-L58	thon	-eva		L77-L78	thon	-eva		L97-L98	thon	-eve		thon
Colf	<b>M</b> 05	L19-L20	M+a	N Self		L39-L40	M+a	Self	M15		M+a	Self		L79-L80	M+a	Self		L99-L100	M+a	Self	M30 L119-L120	M+a
JEMM+athon 1		JEM	JEMM+athon 2		JEMM+athon 3		JEMM+athon 4		JEM		JEMN	A+athon 5	JEMI		JEMM+athon 6	JEMI						

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EM	<b>EMM</b> L01-L20		<b>EMM</b> L21-L40				<b>EMM</b> L41-L60			EMM L61-L80				EMM L81-L100					
	M01	L11-L12	Ш		M06	L31–L32	Ш		M11	L51–L52	Ш		M16	L71–L72	ш		M21	L91-L92	Ш
ы	M02	L13-L14	GFR	u	M07	L33-L34	GFR	ы	M12	L53-L54	GFR	ы	M17	L73–L74	GFR	ы	M22	L93-L94	GFR
luati	M03	L15-L16	0 BU	luati	M08	L35-L36	0 BU	luati	M13	L55-L56	0 BL	luati	M18	L75–L76	0 BL	luati	M23	L95-L96	BU
-eva	M04	L17-L18	on to	-eva	M09	L37–L38	on to	-eva	M14	L57–L58	onte	-eva	M19	L77–L78	on to	-eva	M24	L97-L98	on to
Self	M05	L19-L20	Aath	Self	M10	L39-L40	Aath	Self	M15	L59-L60	Aath	Self	M20	L79–L80	Nath	Self	M25	L99-L100	Aath
	EMMathon 1			EMM	Aathon 2	EM		EMM	Aathon 3	EM		EMI	Mathon 4	EM		EM	Mathon 5	EMP	

Year 6						
EMM L01-L20 EMM L21-L40	EIMI L41-L60 M11 L51-L52 M12 L53-L54 M13 L55-L56 M15 L59-L60 M15 L59-L60 M15 L59-L60	EMM L61–L80 M16 L71–L72 M17 L73–L74 M18 L75–L76 M20 L75–L76 M20 L79–L80 M20 L79–L80 M21 M21 EMMathon 4	EMM L81-L100 M21 L91-L92 H M22 L93-L94 H M23 L95-L96 9 M24 L97-L98 0 M25 L99-L100 H EMMathon 5 H	EMM L101-L120 M26 L111-L112 M27 L113-L114 M28 L115-L116 M30 L119-L120 M30 L19-L120 EMMathon 6 M3	EMM L121-L140 M31 L131-L132 M32 L133-L134 M33 L135-L136 M35 L139-L140 M35 L139-L140 M35 L139-L140 M35 L139-L140	EMM L141-L160 M36 L151-L152 U M37 L153-L154 M38 L155-L156 U M39 L157-L158 U M40 L159-L160 U EMMathon 8

Year 7							
EMM L01-L20	EMM L21-L40	Self-evaluation	Self-evaluation	EMM 1.81–1.100 M21 1.91–1.92 M22 1.93–1.94 M23 1.95–1.96 M24 1.97–1.98 M25 1.99–1.100 EMMathon 5	EMM L101–L120 M26 L111–L112 M27 L113–L114 M28 L115–L116 M29 L117–L118 M29 L117–L118 M30 L119–L120 EMMathon 6	EMM L121-L140 M31 L131-L132 M32 L133-L134 M33 L135-L136 M34 L137-L138 M35 L139-L140 EMMathon 7	EMM 1/14/-1/160 M36 1/15/-1/152 M37 1/153-1/154 M38 1/155-1/156 M39 1/157-1/158 M40 1/159-1/160 EMMathon 8

## **SUGGESTED IMPLEMENTATION PLAN:** Special needs Yr 3, 4, 5, 6, 7 and 8

Programs at each year level must be commenced at Lesson 1, and must be completed, before moving on to the next program. The following plan illustrates the stages at which the JEMMathons, JEMM+athons, and EMMathons commence. For example, Year 7 students complete lessons 1–60 before doing their first EMMathon.

Note: Low-performing students would benefit from completing all JEMMathons, JEMM+athons, and EMMathons.

Year 3 and Year	4						
JEMIN L01-L20 M01 L01-L04 M02 M02 L05-L08 M03 L09-L12 M04 L13-L16 M05 L17-L20 JEMINathon 1	JEMM L21–L40 M06 L21–L24 H44 M07 L25–L28 M08 L29–L32 M09 L33–L36 00 00 00 00 00 00 00 00 00 00 00 00 00	JEMM L41-L60 M11 L41-L44 H12 L45-L48 H13 L45-L48 H13 L49-L52 H14 H13 L49-L52 H14 H14 L53-L56 H15 L57-L60 H15 H15 L57-L60 H15 H15 L57-L60 H15	JEMM L61–L80 M16 L61–L64 H M17 L65–L68 M M17 L65–L68 M M19 L73–L76 M M20 L77–L80 M JEMMathon 4				
Year 5							
JEMM+ L01-L20 M01 L11-L12 Hardree for the second s	JEMM+ L21–L40 M06 L31–L32 H44 M07 L33–L34 M07 L33–L34 M08 L35–L36 uoqta M10 L39–L40 H44 JEMM+athon 2 J	JEMM+ L41–L60 M11 L51–L52 H44 M12 L53–L54 M13 L55–L56 quot M15 L59–L60 M15 L59–L60 JEMM+athon 3	JEMM+ L61−L80 M16 L71−L72 H4450 M17 L73−L74 M18 L75−L76 Q M20 L79−L78 M20 L79−L80 JEMM+athon 4	JEMM+ L81-L100 M21 L91-L92 H84-50 M22 L93-L96 quot M23 L95-L96 quot M25 L99-L100 JEMM+athon 5	JEMM+ L101-L120		
Year 6							
Self-evaluation	JEMM+ L21-L40	JEMM+ L41–L60 M11 L51–L52 M12 L53–L54 M13 L55–L56 M14 L57–L58 M14 L57–L58 M15 L59–L60 JEMM+athon 3	JEWM+ L61–L80   M16 L71–L72 Hutton   M17 L73–L74 Hutton   M18 L75–L76 Hutton   M19 L77–L78 Hutton   M20 L79–L80 Hutton   JEMM+athon 4 JEMM JEMM	JEMM+ L81-L100 M21 L91-L92 M22 L93-L94 M23 L95-L96 M24 L97-L98 M25 L99-L100 JEMM+athon 5	JEMM+ L101-L120 M26 L111-L112 HH M27 L113-L114 098 M28 L115-L116 098 M29 L117-L118 098 M30 L119-L120 HH JEMM+athon 6	EMM L01-L20 M01 L11-L12 H M02 L13-L14 H M03 L15-L16 0 M04 L17-L18 0 M05 L19-L20 EMMathon 1	EMM L21-L40 M06 L31-L32 H M07 L33-L34 H M08 L35-L36 A M09 L37-L38 H M10 L39-L40 H M10 L39-L39 H M10 L39-L40 H M10 L39-
Year 7							
EMM L01-L20	EMM L21-L40	EMM L41-L60   M11 L51-L52 H11   M12 L53-L54 H11   M13 L55-L56 H11   M14 L57-L58 H115   M15 L59-L60 HH44	L61-L80   M16 L71-L72 H19   M17 L73-L74 H19   M19 L77-L78 H19   M20 L79-L80 H14	EMM L81-L100   M21 L91-L92 H   M22 L93-L94 H   M23 L95-L96 H   M24 L97-L98 H   M25 L99-L100 H   M25 L99-L100 H	EMM L101–L120 M26 L111–L112 M27 L113–L114 M27 L113–L114 M28 L115–L116 M29 L117–L118 M29 L117–L118 M30 L119–L120 EMMathon 6	EMM L121-L140 M31 L131-L132 M32 L133-L134 M33 L135-L136 M34 L137-L138 M34 L137-L138 M35 L139-L140 EMMathon 7	EMM L141-L160 M36 L151-L152 H M37 L153-L154 M38 L155-L156 U M39 L157-L158 M40 L159-L160 U EMMathon 8
Year 8							
Soft-evaluation	EMM L21-L40	EMM L41-L60	Seff-evaluation Seff-evaluation	L81-L100   M21 L91-L92   H22 L93-L94   H23 L95-L96   M24 L97-L98   M25 L99-L100   M25 L99-L94   H23 H95-L96   M24 L97-L98   M25 L99-L100   H25 L99-L100	EMM L101-L120 M26 L111-L112 UM27 L113-L114 W28 L115-L116 M29 L117-L118 M30 L119-L120 M30 L119-L120 EMMathon 6	EMM L121-L140 M31 L131-L132 M32 L133-L134 M33 L135-L134 M34 L137-L138 M35 L139-L140 EMMathon 7	EMM L141-L160 M36 L151-L152 H1450 M37 L153-L154 H1450 M38 L155-L156 Q M39 L155-L156 Q M39 L157-L158 M40 L159-L160 EMMathon 8

## **PLACEMENT INTO PROGRAM**

Because EMM assumes nothing in terms of student academic level, it is important that all students enter the program at Lesson 1. If students achieve an overall success rate of 100% in the first two Rounds (Lessons 1–10), continue the program presenting the questions only. Once student overall success rate in a Round drops below 95%, return to the beginning of the previous Round and repeat those lessons using the entire script.

## **PREPARING TO TEACH EMM**

Read pages i – xvi, and then familiarise yourself with the script by reading the first Round (Lessons 1–5). Set up and check electronic equipment for ERS. If using a non-electronic delivery, prepare copy (A3 or larger) of *Colour Masters* (see below). If you are not using the myEMMdata Student Workbook, have students prepare workbooks for Round 1 (see page xv) prior to commencing the program.

When introducing students to EMM explain that in the beginning lessons they will be working with basic skills they probably already have, however, in order to meet the challenges ahead they will need to become fluent (able to respond accurately and without hesitation) and automatic (able to respond without conscious attention) with these skills. Go to Lesson 146 and present Question 20 by way of example. Go next to Lesson 21 and present Section 5 to demonstrate the manner in which you will be delivering the lessons. Explain the lesson structure.

## **LESSON STRUCTURE**

15–20 min: Intensive teacher-directed instruction

Using script, teacher models at a brisk pace, but not too fast. Each sentence should be delivered in small chunks. For example: "The difference between two numbers" *pause* "tells how much more or less" *pause* "one number is than the other."

#### No interruptions-student focus must be on the teacher.

Teacher poses a question for each strand. Length of time for student response depends on degree of difficulty – could be as little as 5 seconds. Students respond by writing answer in the column assigned to that lesson. Students may do calculations on the facing page.

- 1–2 min: Corrections
- 4–8 min: DEBUG (see page xi)

## **SCHEDULED TIME**

Lessons should be scheduled daily. Generally speaking by Round 6 (Lessons 26–30) an EMM lesson should take no more than 25 minutes.

## **COLOUR MASTERS (Non-electronic delivery only)**

Teachers are advised to print and laminate an A3 size copy of each Colour Master before commencing the MMS. The Colour Masters found on the ERS should be displayed prior to the lesson. These Masters replicate the snapshots shown in the lessons. They contain detailed board work that may be time-consuming for the teacher to write up.

## FOR THOSE NOT USING PRESCRIBED WORKBOOK

Ideally use a 96 page exercise book. There are 160 lessons or 32 rounds. For diagnostic purposes (see Corrections page xi) each round of 5 lessons should be contained within a double-page spread.



Each right-hand page should be ruled as shown in the myEMMdata Student Workbook (see snapshot above). The right-hand page is for recording answers, one column per lesson. If students miss a lesson the column should be left blank until they catch up. The left-hand page is for rough working out.

## **AUTHOR'S NOTE**

The student-directed versus teacher-directed learning debate is an ancient one; indeed, the polemic goes back to Plato. In her doctoral research: https://doi.org/10.4225/03/586eef2192323 the author carried out a comprehensive review of the relevant research and literature, and reached the inescapable conclusion that some skills were better acquired through one approach, and some through the other. When it came to the employment and cultivation of higher order skills, where reasoning and reflection were required, it was clear that a student-directed approach to learning was better suited. But when it came to the acquisition of basic skills, the empirical evidence unequivocally showed that a teacher-directed approach won out.

It is well accepted that problem solving skills operate from a knowledge base that has been acquired through practice; in fact, genuine competence in both problem solving and basic skills *only* comes with practice. Significantly though, it is actually when the base knowledge in a discipline is being acquired that the foundations for effective problem solving are being laid. Because the essential knowledge required for automaticity is stored in long term memory, it is best retained when explicitly taught and practised repeatedly. This automaticity, originating from practice, empowers students to maximise their mental capacity by concentrating exclusively on the more complex task of problem solving.

It is also well accepted that to perform a task competently one requires not only the requisite skills, but also the self-belief in one's ability to implement performance. In the learning process this is termed *self-efficacy*, and when laying the foundational skills in mathematics, or for that matter any academic discipline, it is important that student self-efficacy be accommodated. Students with low self-efficacy in a particular skill area are reluctant to engage in tasks where those skills are required, and if they do, they are more likely to quit when encountering difficulty.

Students engaged in the learning process automatically monitor their progress. For this reason the capacity to self-evaluate progress is an integral and ongoing component of the EMM program. Because EMM tasks gradually increase in difficulty, students have clear criteria by which they can independently assess their performance and gauge their progress. As they progress they acquire more skills and become more proficient at the self-evaluation process.

EMM lessons were deliberately designed not to be seen as tests, but testing is precisely what is happening on a daily basis. Without being conscious of it, students are willingly engaging in ongoing assessment. As such the lessons serve as a powerful diagnostic tool clearly mapping student progress, identifying precisely where and when they are experiencing difficulty. Their responses, coupled with their own analysis of any incorrect response they have given during a lesson, provide teachers with reliable diagnostic information better than any that can be acquired from a formal test situation. This is crucial to EMM's success as it allows for teacher feedback to specifically target individual student misunderstanding. Because students receive this daily feedback on their performance, they are acutely and immediately aware of their progress, which strengthens their self-efficacy, sustains their motivation, and enhances their academic achievement.

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