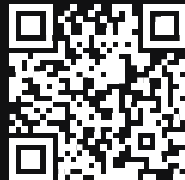


The background is a vibrant, abstract composition of colorful light trails in shades of green, purple, yellow, and blue, swirling and radiating from various points. Overlaid on these trails are faint, semi-transparent mathematical symbols, including a red triangle, a blue square, and a green circle with a cross inside. The overall effect is dynamic and futuristic.

Welcome to
MATH MASTERY SERIES™

Presented by Dr Rhonda Farkota



Direct Instruction (DI)

Little to Chance — Much to Gain
Math Mastery Series

Professor John Hattie

Melbourne University

Director, Melb Ed Research Institute (MERI) and Associate Dean (Research)

Too often, what the critics mean by direct instruction is didactic teacher-led talking from the front; this should **not** be confused with the very successful Direct Instruction method as first outlined by Adams and Engelmann (1996).

... the underlying principles of DI place it among the most successful outcomes.

Visible Learning: A synthesis of over 800 meta-analyses relating to achievement (2009)
pp204–205. Routledge ISBN 10:0-415-47618-6

...the influences on student achievement – what works best for students

The background is a solid orange color with a complex, abstract pattern. It features a large, faint spiral in the center, surrounded by various mathematical sketches and diagrams, including triangles, circles, and lines, all rendered in a lighter shade of orange. The overall effect is a textured, artistic representation of mathematics.

Overview

Math Mastery Series

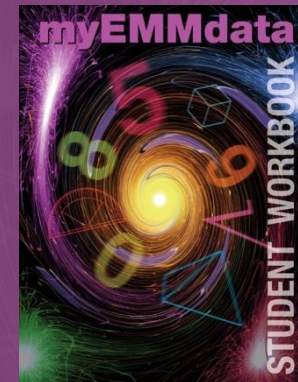
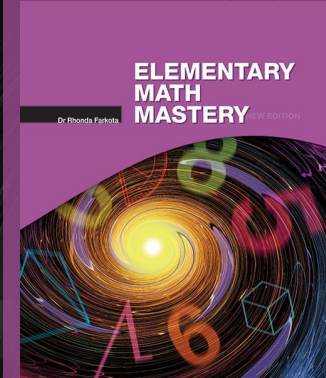
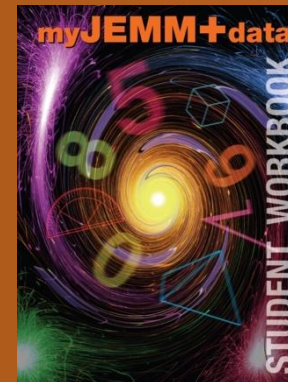
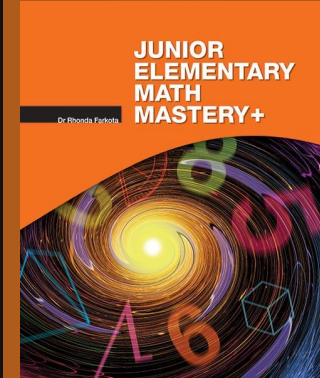
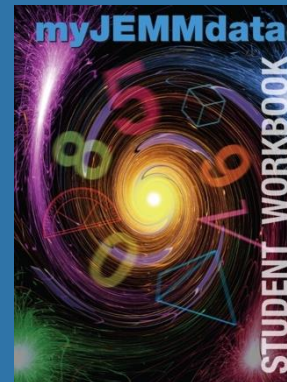
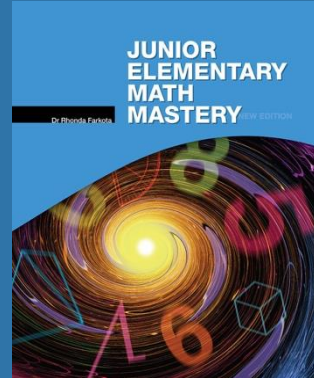
Math Mastery Series

Farkota DI Model for the contemporary
Australian classroom

Direct Instruction
approach to basic skills
fluency and
automaticity

Data driven

Teachers: Deliver Diagnose DeBug
Students: Record Represent Report



Math Mastery Series



- Orally delivered
- Imparts skills and knowledge in progressive order
- Enables teachers and students to identify exactly where and when students experience difficulty
- Serves as a daily diagnostic tool

Electronic Reference Stimuli (ERS)

all visual diagrams, formulas and display material

- Provides effortless visual delivery
- Enhances student engagement
- Aids low-ability students
- Maximises time-efficiency

Lesson 1

Question 1

									0
1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	52	53	54	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
91	92	93	94	95	96	97	98	99	100
101	102	103	104	105	106	107	108	109	110

Lesson 1

Question 2

$$\begin{array}{r} \text{addend} \\ \hline 7 \\ \hline \end{array} + \begin{array}{r} \text{addend} \\ \hline 3 \\ \hline \end{array} = \begin{array}{r} \text{sum} \\ \hline 10 \\ \hline \end{array}$$

1	2	3	4	5	6	7	8	9	10
---	---	---	---	---	---	---	---	---	----

10	9	8	7	6	5	4	3	2	1
----	---	---	---	---	---	---	---	---	---

1	2	3	4	5	6	7	8	9	10
---	---	---	---	---	---	---	---	---	----

Student Workbook

Monitors quality of implementation tracking teacher performance and student achievement

Daily students **record**, **summarise** and **represent** their own data

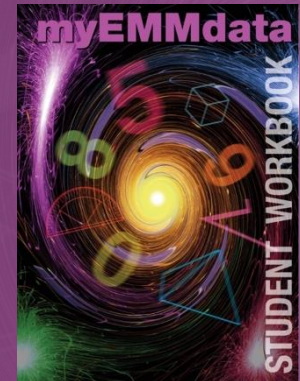
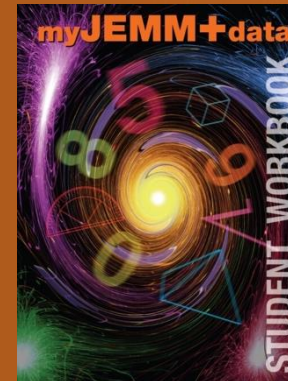
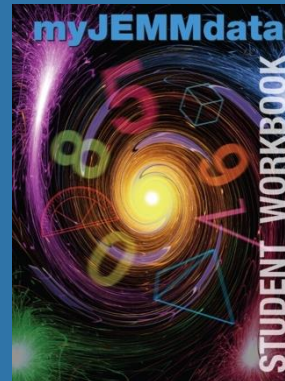
Data driven

Teachers:

Students :

Deliver Diagnose DeBug

Record Represent Report



Math Mastery Series

- Lessons presented orally
- Auditory processing capacity

...the ability of the child to hold, sequence and process or understand what they have heard

Pollard J., Rowe K. S

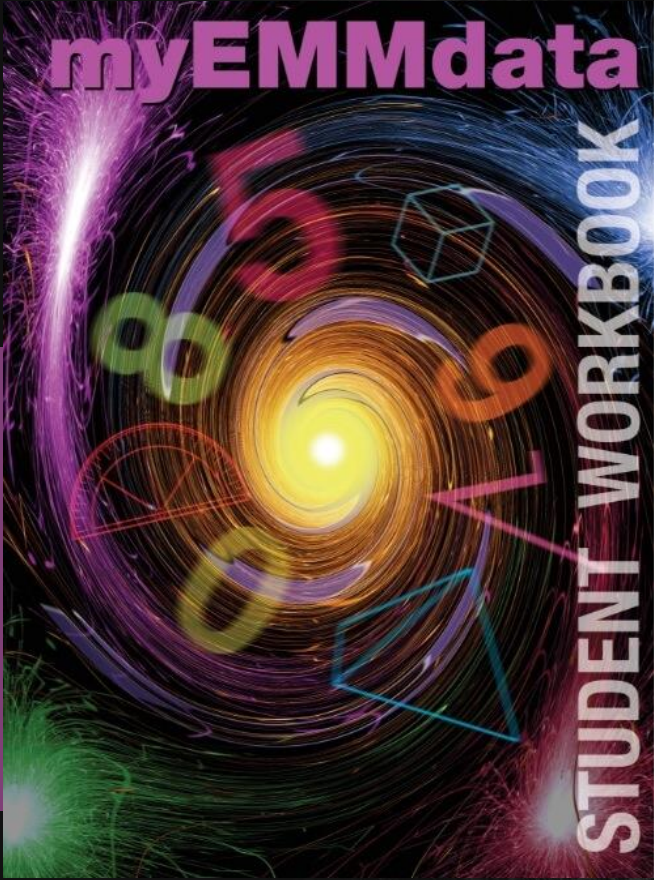
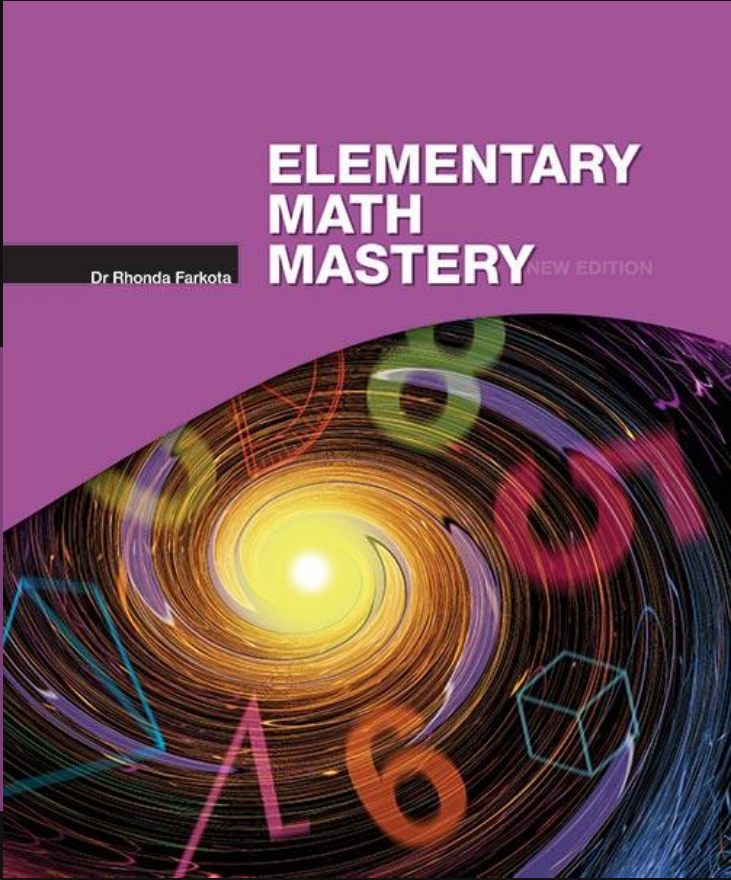
<http://auditoryprocessingkit.com/auditory-processing-101.php>

Math Mastery Series

	Number of sessions to complete MMS			
	EMM	JEMM+	JEMM	TOTAL
Teacher delivered scripted lessons	160	120	80	360
Student Self-evaluations	8	6	4	18
Marathons	40	30	20	90
EMM/JEMM+/JEMMathon tasks	8	6	4	18
Round tasks	24	18	12	54
Challenges	4	4	4	12
TOTAL number of sessions required	244	184	124	552

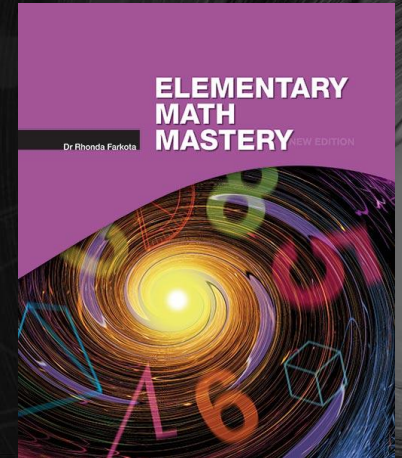
The background is a solid purple color with faint, light-colored mathematical sketches overlaid. These sketches include a circle with a radius line, a triangle, a square, and a hexagon. The text is white and positioned on the left side of the image.

Elementary Math Mastery (EMM)



EMM

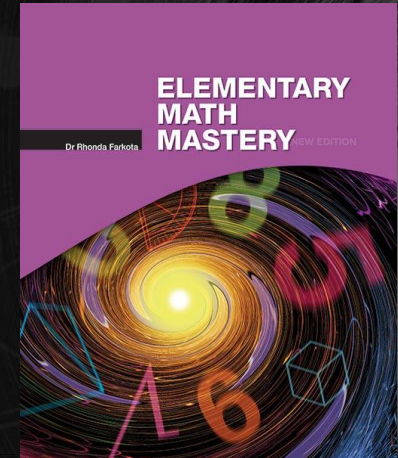
- Ideally suited to upper primary, secondary and remedial students
- Requires 20–25 min daily to implement + 5–10 min for correction and feedback
- 3200 questions
- 160 lessons
- 20 strands each lesson



20 EMM Strands

- ✓ addition
- ✓ subtraction
- ✓ multiplication
- ✓ division
- ✓ number patterns
- ✓ equations and inverse operations
- ✓ whole number properties
- ✓ fractions
- ✓ decimals
- ✓ measurement
- ✓ space
- ✓ geometry
- ✓ average, percentage, ratio, chance
- ✓ math language
- ✓ money
- ✓ time
- ✓ algebra
- ✓ visual perception
- ✓ data analysis
- ✓ problem solving

fluency
automaticity



Program Structure – EMM

160 lessons starting at base level structured in rounds of five

New concepts introduced in first lesson of round

Last lessons of each round put these concepts to the test

The screenshot displays the EMM program interface, divided into two main sections: WORKSPACE and DAILY DATA.

WORKSPACE: This section shows a vertical list of lessons grouped into rounds. Round 1 includes Lesson 1, Lesson 2, Lesson 3, Lesson 4, and Lesson 5. The lessons are represented by colored bars.

DAILY DATA: This section contains a table for recording student performance. The table has columns for Date, Round, Lesson 1 through Lesson 5, and a BugBoard with columns 1 through 5. The rows represent questions 1 through 20. Below the table, there is a 'Visual representation' section with five bars of varying heights, each representing a lesson's score. A ruler is also visible at the bottom left of the workspace area.

Annotations: Three purple arrows point from the text on the left to the corresponding parts of the interface: the first arrow points to the 'Lesson 1' bar in the workspace; the second arrow points to the 'Lesson 1' column in the 'DAILY DATA' table; the third arrow points to the 'Lesson 5' column in the 'DAILY DATA' table.

Page Information: The bottom left of the workspace area shows the page number '2' and the text 'myEMMdata'. The bottom right of the 'DAILY DATA' area shows the page number '3' and the text 'DAILY DATA ROUND 1'.

Text in the workspace area:

For each Lesson the whole of my data is represented in a bar made of 20 rectangles. From the baseline, I summarise my data by shading the number of rectangles equal to my score.

After recording and summarising my data for these 5 lessons, I go to page 10 and complete my task for this Round.

WORKSPACE

Lesson 131

$$\begin{array}{r} 423124 \\ +423524 \\ \hline 846648 \end{array}$$

$$\frac{24}{4} = \frac{1}{3} \quad \frac{24}{2} \quad 10m = 30s$$

$$\begin{array}{r} 5890 \\ -1194 \\ \hline 4496 \end{array}$$

$$\frac{24}{6 \times 4 = 24cm^2} \quad \frac{85}{1.90} \quad 4 \times 4 = 16$$

Lesson 132

$$\begin{array}{r} 434321 \\ +434521 \\ \hline 868842 \end{array}$$

$$\frac{27}{27} = 3 \quad 9 \times 6 = 54cm^2$$

$$\frac{27}{3} = 9 \quad 95 \times 10 = 950$$

$$\frac{27}{4} = \frac{3}{5} \quad 10m = 30s$$

$$20m = 60s$$

Lesson 133

$$\begin{array}{r} 441232 \\ +441772 \\ \hline 883004 \end{array}$$

$$\frac{24}{24} = 5 \times 8 \quad 10m = 30s$$

$$\frac{24}{5} = 4 \frac{4}{5} \quad 20m = 60s = 1km$$

Lesson 134

$$\begin{array}{r} 435244 \\ +435844 \\ \hline 871088 \end{array}$$

$$\frac{63}{63} = 2 \quad 48 - 12 = 24 \div 6 = 4$$

$$\frac{63}{2} = 31 \frac{1}{2} \quad \frac{24}{6} = 4$$

Lesson 135

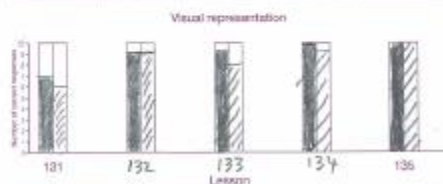
$$\begin{array}{r} 437142 \\ +437542 \\ \hline 874684 \end{array}$$

$$\frac{15}{15} = 3 \quad 3cm^2 \times 6 = 18cm^2$$

For each Lesson the whole of my data is represented in 2 columns. The first column represents Question group 1-10. For this group I colour code the KEY. Next I fill in the missing labels. Then I shade the column upwards stopping at the number equal to the number of my correct responses. I repeat the process for Question group 11-20.

DAILY DATA

Date	3-12-12	4-12-12	5-12-12	6-12-12	7-12-12	BugBoard					
Round 27	Lesson 131	Lesson 132	Lesson 133	Lesson 134	Lesson 135	131	132	133	134	135	
Question 1	846648	868842	883004	871088	874684	☺	☺	☺	☺	☺	1
Question 2	4496	2196	6296	8496	5396	☺	☺	☺	☺	☺	2
Question 3	+	-	⊖	28 +	(9150) +	☺	☺	☺	☺	☺	3
Question 4	17	9	4 $\frac{4}{5}$	31 $\frac{1}{2}$	11	☺	☺	☺	☺	☺	4
Question 5	30	15	9	63	29	☺	☺	☺	☺	☺	5
Question 6	⊖	-	-	+	÷	☺	☺	☺	☺	☺	6
Question 7	2	3	5	4	10	☺	☺	☺	☺	☺	7
Question 8	$\frac{1}{3}$	$\frac{3}{3}$	$\frac{1}{5}$	$\frac{1}{3}$	$\frac{1}{3}$	☺	☺	☺	☺	☺	8
Question 9	12%	14	$\frac{2}{100}$	5%	9/100	☺	☺	☺	☺	☺	9
Question 10	200	500ML	1g	201g	210g	☺	☺	☺	☺	☺	10
Question 11	6	6	c	a	b	☺	☺	☺	☺	☺	11
Question 12	24cm	54cm ²	6cm ²	12cm ²	13cm ²	☺	☺	☺	☺	☺	12
Question 13	Tail	Head	2	3	1h, 1t	☺	☺	☺	☺	☺	13
Question 14	2	10	3	4	5	☺	☺	☺	☺	☺	14
Question 15	10	12	2	18	12	☺	☺	☺	☺	☺	15
Question 16	3	60sec	1	2min	1.2km	☺	☺	☺	☺	☺	16
Question 17	15	6	30	10	25	☺	☺	☺	☺	☺	17
Question 18	East	North	South	North	SE	☺	☺	☺	☺	☺	18
Question 19	(9, 8)	(8, 6)	Pond	Pond	Bulb	☺	☺	☺	☺	☺	19
Question 20	16	16	12	$\frac{1}{2}$	$\frac{5}{2}$	☺	☺	☺	☺	☺	20
My score	13	18	17	19	20						
Out of	20	20	20	20	20						



After recording and summarising my data, I go to page 98 and complete my task for the Round.

What bugs you?

- BUG - incorrect response where student is unable to understand why they are wrong
- DEBUG directly after corrections
- Do not debug EMM Question 20, JEMM+ Question 15, JEMM Strategic Thinking Units



What bugs you?

.... brilliant teachers identify problems before they happen. And, the debugging process that is used in the Math Mastery Series (EMM, JEMM, JEMM+) is a great example of a timely correction process (see Boyd, MacNeill, & Sullivan, 2019).

DR RAY BOYD AND DR NEIL MACNEILL

EDUCATION TODAY FEB 10, 2023

<https://www.educationtoday.com.au/news-detail/Explicit-Instruction-5836>

Lesson 21 – Teacher Script

Scripts indicate what you say, do, and display

What you stress is in **bold text**.

What you say appears in this type.

What you say and simultaneously point at on the electronic display or whiteboard appears in **CAPITAL LETTERS**.

13 Refer to ERS Question 13.

SNAPSHOT

part A 1 square
part B 3 squares

The **average** tells how many there would be in each part if the total sum were evenly shared.

PART A is one part and **PART B** is the other part.

QUESTION 13 How many parts altogether? (Repeat question)

What you do appears in *italics*.

L21

Lesson 21

Display ERS Lesson 21 and 1 m ruler.

1 Refer to ERS Question 1.

SNAPSHOT
6 4 5
+ 2 3 7
— 8 2

With some addition problems you need to carry. Start with the ones column: **FOUR** plus **SEVEN** equals **TEN**.

TEN has digits so write the ones digit, **TWO**, as the answer for the ones.

Carry the **ONE TEN** to the tens. **FOUR** plus **THREE** equals **SEVEN**. Add the **ONE** carried equals **EIGHT** tens altogether.

Write the answer **EIGHT** in the tens column. Then continue as you usually do.

QUESTION 1

Find the sum of 645 and 237. (Repeat question)

2 Refer to ERS Question 2.

SNAPSHOT
6 4 5
- 2 3 7
— 0 8

When you can't work a subtraction problem in a column, you rename.

FIVE minus **SEVEN** begins with a smaller number and you can't work it.

Take 1 ten from the tens digit **FOUR**. That leaves **THREE** tens.

Change the **ONE TEN** into ones making a total of **FIFTEEN ONES**.

FIFTEEN minus **SEVEN** equals **EIGHT**.

The new problem in the tens column is **THREE** minus **THREE** equals **ZERO**.

QUESTION 2

645 minus 237. (Repeat question)

3 Refer to ERS Question 3.

SNAPSHOT
6 4
× 4
— 1 8 4

Here's **FOURTY-SIX** multiplied by **FOUR**. Start with the ones column: **FOUR** by **SIX** equals **24**. Write **FOUR** as the answer for the ones.

FOUR by **FOUR** equals **16**, add the **TWO** tens carried equals **EIGHTEEN** tens altogether.

QUESTION 3 Multiply 24 by 5. (Repeat question)

4 Display ERS Question 4. Apart from identifying lesson and question number the slide is blank – the object of the display is simply to keep students on track.

QUESTION 4

804 divided by 4. (Repeat question)

5 Refer to ERS Question 5.

SNAPSHOT
6 4 5
9
1 8
2 7
3 6
4 5

When counting in five the first five numbers are **NINE**, **EIGHTEEN**, **TWENTY-SEVEN**, **THIRTY-SIX**, **FORTY-FIVE**.

Look at the **ONES** digit of each number. **NINE**, **EIGHT**, **SEVEN**, **SIX**, **FIVE**.

QUESTION 5 When counting in five what number does the ones digit decrease by? (Repeat question)

6 Refer to ERS Question 6.

SNAPSHOT
2 4 + 8 8 + 4 = 2

Here's a **MULTIPLICATION FACT** and related **DIVISION FACT**.

The division fact starts with the **larger number**. (Repeat question)

QUESTION 6

Copy the division fact. (Repeat question)

7 Refer to ERS Question 7.

SNAPSHOT
7 6 1 9 3

QUESTION 7 Rearrange the **DIGITS** to make the **largest number possible**. (Repeat question)

8 Refer to ERS Question 8.

SNAPSHOT
 $\frac{1}{2} + \frac{1}{2} = 1$

The fraction for this picture is **THREE-HALVES**. A mixed number has a **whole number** and a **fraction**. The number of wholes used up is **ONE**. The fraction which talks about the whole not used up is **ONE-HALF**.

The mixed number is **ONE AND ONE-HALF**. (Repeat question)

QUESTION 8

Write the mixed number for this picture. (Repeat question)

QUESTION 9 Display ERS Question 9. Apart from identifying lesson and question number the slide is blank – the object of the display is simply to keep students on track.

QUESTION 9

Write the decimal number 51 and 2 tenths. (Repeat question)

10 Refer to ERS Question 10 and 1 m ruler.

SNAPSHOT
0 1 2 3 4 5 6 7 8 9 10
No to scale

1000 m = 1 km
Distance is measured in kilometres. **ONE THOUSAND METRES** EQUALS **ONE KILOMETRE**.

A **SMALL KM** is the sign for kilometre.

QUESTION 10

If it takes 1000 **ROLLERS** and to end, what will be their total length in kilometres? (Repeat question)

11 Refer to ERS Question 11.

SNAPSHOT
▲

An **EQUILATERAL** triangle has all sides equal in length. The **DASH** indicates sides of equal length.

QUESTION 11 Write the name used to describe a triangle with all sides equal in length. (Repeat question)

L21

12 Refer to ERS Question 12.

SNAPSHOT
▲
P = 6 cm

The perimeter of an equilateral triangle is **SIX CENTIMETRES**. Divide the perimeter by 3 to find the length of each side.

QUESTION 12

The perimeter of an equilateral triangle is 6 centimetres. What is the length of each side? (Repeat question)

13 Display ERS Question 13. Apart from identifying lesson and question number the slide is blank – the object of the display is simply to keep students on track.

QUESTION 13

A truck travels 50 km in 1 hour. A car travels 60 km in 1 hour. Which has the greater average speed? (Repeat question)

14 Refer to ERS Question 14.

SNAPSHOT
20 ÷ 5 = 4

The quotient is the result after dividing. In the division 20 divided by 5, **FOUR** is the quotient.

QUESTION 14

Find the quotient of 15 divided by 3. (Repeat question)

15 Display ERS Question 15. Apart from identifying lesson and question number the slide is blank – the object of the display is simply to keep students on track.

QUESTION 15

How much change from \$5.15 if I spent \$4.50? (Repeat question)

16 Display ERS Question 16. Apart from identifying lesson and question number the slide is blank – the object of the display is simply to keep students on track.

QUESTION 16

How many hours have passed between midnight and noon? (Repeat question)

17 Refer to ERS Question 17.

SNAPSHOT
130 × 10 = 13

This number sentence says divide **ONE HUNDRED AND THIRTY** by **TEN** and you get **THIRTEEN**.

QUESTION 17

Write the number sentence for this fact: divide 200 by 25 and you get 8. (Repeat question)

18 Refer to ERS Question 18.

SNAPSHOT
□
X Y Z

QUESTION 18 **Y** is halfway between **X** and **Z**. What fraction of the rectangle is shaded? (Repeat question)

19 Refer to ERS Question 19.

SNAPSHOT
Springville Infant School

	Grade two	Grade one	Total
Girls	11	14	25
Boys	28	25	53
Total	39	39	78

Look at the **TABLE**.

QUESTION 19

Calculate how many boys are in Grade two. (Repeat question)

20 Display ERS Question 20. Apart from identifying lesson and question number the slide is blank – the object of the display is simply to keep students on track.

QUESTION 20

A cork and bottle costs \$4.20. The bottle costs \$4 more than the cork. Find the cost of the cork. (Repeat question)

Correct all questions. **DEBUO** directly after corrections.

ANSWER KEY

21.1	882	21.11	Equilateral
21.2	406	21.12	2 cm
21.3	100	21.13	Car
21.4	201	21.14	5
21.5	One (1)	21.15	\$1.05
21.6	8 + 4 = 2	21.16	12 hours
21.7	97 631	21.17	200 × 25 = 8
21.8	$\frac{1}{2}$	21.18	$\frac{1}{2}$
21.9	51.2	21.19	14
21.10	1 km	21.20	10c

Number Patterns – Question 5

Number Patterns Continuum

- ✓ 2s counting
Divisibility test Application
- ✓ 5s counting
Divisibility test Application
- ✓ 9s counting
Divisibility test Application
- ✓ 3s counting
Divisibility test Application
- ✓ 10s counting
Divisibility test Application

- ✓ 4s counting
Divisibility test Application
- ✓ 8s counting
Divisibility test Application
- ✓ 25s counting
Money amounts
- ✓ 6s counting
Divisibility test Application
- ✓ Missing number within
pattern

Lesson 21 – Teacher Script

Scripts indicate what you say, do, and display

L21

Lesson 21

Display ERS Lesson 21 and 1 m ruler.

1 Refer to ERS Question 1.
SNAPSHOT

$$\begin{array}{r} 645 \\ + 237 \\ \hline 882 \end{array}$$
 With some addition problems you need to carry. Start with the ones column: FIVE plus SEVEN equals 12. 12 has two digits so write the ones digit, TWO, as the answer for the ones. Carry the ONE TEN to the tens. FOUR plus THREE equals 7, add the ONE carried equals EIGHT tens altogether. Write the answer EIGHT in the tens column. Then continue as you usually do.
QUESTION 1 Find the sum of 645 and 237. (Repeat question)

2 Refer to ERS Question 2.
SNAPSHOT

$$\begin{array}{r} 645 \\ - 237 \\ \hline 408 \end{array}$$
 When you can't work a subtraction problem in a column, you rename.
 FIVE minus SEVEN begins with a smaller number and you can't work it.
 Take 1 ten from the tens digit FOUR. That leaves THREE tens. Change the ONE TEN into ones making a total of FIFTEEN ONES.
 FIFTEEN minus SEVEN equals EIGHT.
 The new problem in the tens column is THREE minus THREE equals ZERO.
 Then continue as you usually do.
QUESTION 2 645 minus 237. (Repeat question)

3 Refer to ERS Question 3.
SNAPSHOT

$$\begin{array}{r} 4 \\ \times 4 \\ \hline 16 \end{array}$$
 Here's FORTY-SIX multiplied by FOUR. Start with the ones column: FOUR by SIX equals 24. Write FOUR as the answer for the ones. FOUR by FOUR equals 16, add the TWO tens carried equals EIGHTEEN tens altogether.
QUESTION 3 Multiply 24 by 5. (Repeat question)

4 Display ERS Question 4. Apart from identifying lesson and question number the slide is blank – the object of the display is simply to keep students on track.
QUESTION 4 804 divided by 4. (Repeat question)

5 Refer to ERS Question 5.
SNAPSHOT

$$\begin{array}{r} 18 \\ 27 \\ 36 \\ 45 \end{array}$$
 When counting in 9s the first five numbers are NINE, EIGHTEEN, TWENTY-SEVEN, THIRTY-SIX, FORTY-FIVE.
 Look at the ONES DIGIT of each number. NINE, EIGHT, SEVEN, SIX, FIVE.
QUESTION 5 When counting in 9s what number does the ones digit decrease by? (Repeat question)

6 Refer to ERS Question 6.
SNAPSHOT

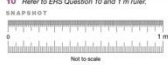
$$2 + 4 = 6 \quad 8 + 4 = 2$$
 Here's a MULTIPLICATION FACT and related DIVISION FACT.
 The division fact starts with the larger number.
QUESTION 6 Copy the division fact. (Repeat question)


7 Refer to ERS Question 7.
SNAPSHOT
 76193
QUESTION 7 Rearrange the DIGITS to make the largest number possible. (Repeat question)

8 Refer to ERS Question 8.
SNAPSHOT

$$\frac{1}{2} + \frac{1}{3} = \frac{5}{6}$$
 The fraction for this picture is THREE-HALVES. A mixed number has a whole number and a fraction. The number of wholes used up is ONE. The fraction which talks about the whole not used up is ONE-HALF. The mixed number is ONE AND ONE-HALF.
QUESTION 8 Write the mixed number for this picture. (Repeat question)


9 Display ERS Question 9. Apart from identifying lesson and question number the slide is blank – the object of the display is simply to keep students on track.

10 Refer to ERS Question 10 and 1 m ruler.
SNAPSHOT

 1000 m = 1 km
 Distance is measured in kilometres. ONE THOUSAND METRES EQUALS ONE KILOMETRE. A SMALL KM is the sign for kilometre.
QUESTION 10 If I place 1000 RULERS end to end, what will be their total length in kilometres? (Repeat question)

11 Refer to ERS Question 11.
SNAPSHOT

 An EQUILATERAL triangle has all sides equal in length. The number of wholes used up is ONE. The DASH indicates sides of equal length.
QUESTION 11 Write the name used to describe a triangle with all sides equal in length. (Repeat question)

← Number Patterns

L21

12 Refer to ERS Question 12.
SNAPSHOT

 P = 6 cm
 The perimeter of an equilateral triangle is SIX CENTIMETRES.
 Divide the perimeter by 3 to find the length of each side.
QUESTION 12 The perimeter of an equilateral triangle is 6 centimetres. What is the length of each side? (Repeat question)

13 Display ERS Question 13. Apart from identifying lesson and question number the slide is blank – the object of the display is simply to keep students on track.

QUESTION 13 A truck travels 50 km in 1 hour. A car travels 60 km in 1 hour. Which has the greater average speed? (Repeat question)

14 Refer to ERS Question 14.
SNAPSHOT

$$20 \div 5 = 4$$
 The quotient is the result after dividing. In this division 20 divided by 5, FOUR is the quotient.
QUESTION 14 Find the quotient of 15 divided by 3. (Repeat question)

15 Display ERS Question 15. Apart from identifying lesson and question number the slide is blank – the object of the display is simply to keep students on track.


QUESTION 15 How much change from \$5.15 I spent \$4.50? (Repeat question)

16 Display ERS Question 16. Apart from identifying lesson and question number the slide is blank – the object of the display is simply to keep students on track.

QUESTION 16 How many hours have passed between midnight and noon? (Repeat question)

17 Refer to ERS Question 17.
SNAPSHOT

$$130 \times 10 = 13$$
 This number sentence says divide ONE HUNDRED AND THIRTY by TEN and you get THIRTEEN.
QUESTION 17 Write the number sentence for this fact: divide 200 by 25 and you get 8. (Repeat question)

18 Refer to ERS Question 18.
SNAPSHOT

 X Y Z
QUESTION 18 Y is halfway between X and Z. What fraction of the rectangle is shaded? (Repeat question)

19 Refer to ERS Question 19.
SNAPSHOT

	Grade two	Grade one	Total
Girls	11	14	25
Boys	26	25	51

 Look at the TABLE.
QUESTION 19 Calculate how many boys are in Grade two. (Repeat question)

20 Display ERS Question 20. Apart from identifying lesson and question number the slide is blank – the object of the display is simply to keep students on track.

QUESTION 20 A cork and bottle costs \$4.20. The bottle costs \$4 more than the cork. Find the cost of the cork. (Repeat question)

Correct all questions.
DEBUG directly after corrections.

	ANSWER KEY	
21.1	882	21.1 Equilateral
21.2	408	21.2 2 cm
21.3	100	21.3 Car
21.4	201	21.4 5
21.5	One (1)	21.5 \$1.05
21.6	8 + 4 = 2	21.6 12 hours
21.7	97 631	21.7 200 + 25 = 8
21.8	12	21.8 2
21.9	51.2	21.9 14
21.10	1 km	21.10 10c

Lesson 21

5 Refer to ERS Question 5.

SNAPSHOT

9
1 8
2 7
3 6
4 5

When counting in 9s the first five numbers are **NINE, EIGHTEEN, TWENTY-SEVEN, THIRTY-SIX, FORTY-FIVE**.

Look at the **ONES DIGIT** of each number.

NINE, EIGHT, SEVEN, SIX, FIVE.

QUESTION 5 When counting in 9s what number does the ones digit **decrease** by? (*Repeat question*)

Students do not see the teacher's script (shown above). Before reaching this stage of the lesson, the teacher presented sections 1 - 4 (addition, subtraction, multiplication and division).

Lesson 21

Question 5

9
1 8
2 7
3 6
4 5

Elementary Math Mastery

Strand development – **first lesson of Round 5**
Section 5: NUMBER PATTERNS
introducing 9s – recognise place value (ones)

Lesson 22

5 Refer to ERS Question 5.

SNAPSHOT

9
1 8
2 7
3 6
4 5

When counting in 9s the first five numbers are **NINE, EIGHTEEN, TWENTY-SEVEN, THIRTY-SIX, FORTY-FIVE.**

Look at the **TENS DIGIT** of each number.
ONE, TWO, THREE, FOUR.

QUESTION 5 When counting in 9s what number does the tens digit **increase** by? (*Repeat question*)

Lesson 22

Question 5

9
1 8
2 7
3 6
4 5

Elementary Math Mastery

Strand development – **second lesson of Round 5**
Section 5: NUMBER PATTERNS
introducing 9s – recognise place value (tens)

Lesson 23

5 Refer to ERS Question 5.

SNAPSHOT

9
1 8
2 7
3 6
4 5

When counting in 9s the first five numbers are **NINE, EIGHTEEN, TWENTY-SEVEN, THIRTY-SIX, FORTY-FIVE.**

QUESTION 5 When counting in 9s the ones digit decreases by 1 and the tens digit increases by 1. When counting in 9s what number comes just **after** 45?
(Repeat question)

Lesson 23

Question 5

9
1 8
2 7
3 6
4 5

Elementary Math Mastery

Strand development – **third lesson of Round 5**
Section 5: NUMBER PATTERNS
Continue 9s pattern

Lesson 24

5 Refer to ERS Question 5.

SNAPSHOT

9
1 8
2 7
3 6
4 5

When counting in 9s the first five numbers are **NINE, EIGHTEEN, TWENTY-SEVEN, THIRTY-SIX, FORTY-FIVE.**

QUESTION 5 When counting in 9s the ones digit decreases by 1 and the tens digit increases by 1. When counting in 9s what number comes just **before** 81? (*Repeat question*)

Lesson 24

Question 5

9
1 8
2 7
3 6
4 5

Elementary Math Mastery

Strand development – *fourth lesson of Round 5*
Section 5: NUMBER PATTERNS
Extend 9s pattern

Lesson 25

5 Refer to ERS Question 5.

SNAPSHOT

9
1 8
2 7
3 6
4 5

When counting in 9s the first five numbers are **NINE, EIGHTEEN, TWENTY-SEVEN, THIRTY-SIX, FORTY-FIVE.**

QUESTION 5 When counting in 9s what number comes just **before** 63, and what number comes just **after** 63 when counting in 9s? (*Repeat question*)

Lesson 25

Question 5

9
1 8
2 7
3 6
4 5

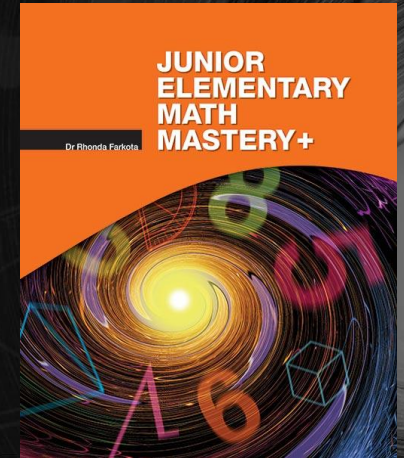
Elementary Math Mastery

Strand development – last lesson of Round 5
Section 5: NUMBER PATTERNS
understanding 9s – put to the test

15 JEMM+ Strands

- ✓ counting
- ✓ addition
- ✓ subtraction
- ✓ multiplication
- ✓ division
- ✓ number patterns
- ✓ fractions
- ✓ decimals
- ✓ measurement
- ✓ space
- ✓ money
- ✓ time
- ✓ visual perception
- ✓ data and chance
- ✓ problem solving

fluency
automaticity

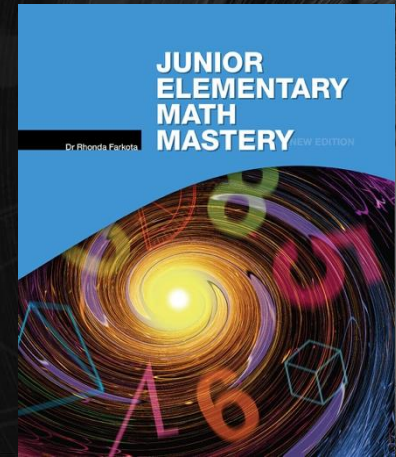


10 JEMM Strands

- ✓ addition
- ✓ subtraction
- ✓ number facts
- ✓ place value
- ✓ number patterns
- ✓ money
- ✓ measurement
- ✓ fractions
- ✓ time
- ✓ data and chance

strategic thinking: a hands-on approach to problem solving

fluency
automaticity



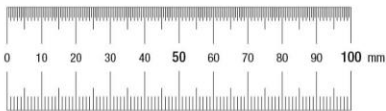
The background is a solid purple color with faint, white, hand-drawn mathematical sketches. These sketches include a circle with a radius line, a triangle, a square, and various lines and curves, suggesting a focus on geometry and mathematics.

myEMMdata Student Workbook

<https://mathmasteryseries.com.au/student-workbook/>

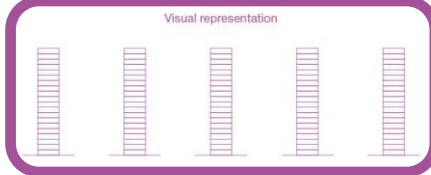
Daily Data: Daily, you record and summarise your own data. For incorrect responses classified as Bugs, you shade the BugKey in the corresponding row on the BugBoard. This allows you and your teacher to monitor your progress.

Visual representation: This provides you with base knowledge and daily practice in reading and interpreting data to prepare you for the Round task.



For each Lesson the whole of my data is represented in a bar made of 20 rectangles. From the baseline, I summarise my data by shading the number of rectangles equal to my score.

	Lesson 1	Lesson 2	Lesson 3	Lesson 4	Lesson 5	BugBoard					
						1	2	3	4	5	
1						☹	☹	☹	☹	☹	1
2						☹	☹	☹	☹	☹	2
3											3
4						☹	☹	☹	☹	☹	4
5						☹	☹	☹	☹	☹	5
6											6
7						☹	☹	☹	☹	☹	7
8											8
9						☹	☹	☹	☹	☹	9
10						☹	☹	☹	☹	☹	10
11						☹	☹	☹	☹	☹	11
12						☹	☹	☹	☹	☹	12
13						☹	☹	☹	☹	☹	13
14						☹	☹	☹	☹	☹	14
15						☹	☹	☹	☹	☹	15
16						☹	☹	☹	☹	☹	16
17						☹	☹	☹	☹	☹	17
18						☹	☹	☹	☹	☹	18
19						☹	☹	☹	☹	☹	19
20						☹	☹	☹	☹	☹	20
	20	20	20	20	20						



After recording and summarising my data for these 5 lessons, I go to page 10 and complete my Task for this Round.

What bugs you?

Feedback originates from the student. When melded with the teachers 'correctional review', feedback becomes a new instruction rather than a mere correction (Kulhavy, 1977). Skilled questioning by the teacher will enhance existing knowledge and 'guide learners to thoughtful and reflective answers' (Samson, Strykowski, Weinstein, & Walberg, 1987).

See next slide for References and suggested reading on Feedback >

References

Hattie, J. (2008). Visible learning pp 173-184 Routledge.

Kulhavy, R. W. (1977). Feedback in Written Instruction. *Review of Educational Research*, 47(2), 211-232.

Samson, G. K., Strykowski, B., Weinstein, T., & Walberg, H. J.(1987). The Effects of Teacher Questioning Levels on Student Achievement: A Quantitative Synthesis. *The Journal of Educational Research*, 80(5), 290–295.

<https://doi.org/10.1080/00220671.1987.10885769>

WORKSPACE

Lesson 131

$$\begin{array}{r} 423124 \\ 7423524 \\ \hline 846648 \\ \hline 5890 \\ -1794 \\ \hline 4496 \end{array}$$

$\frac{1}{4} = \frac{1}{3}$ $\frac{24}{2}$ $10m = 36s$

$$\begin{array}{r} 644-240 \\ \hline 85 \\ \hline 1.90 \end{array}$$

$4 \times 4 = 16$

Lesson 132

$$\begin{array}{r} 434321 \\ 434521 \\ \hline 868842 \end{array}$$

$270 \div 30$ $9 \times 6 = 54 \text{ cm}^2$
 $27 = 3$

Lesson

$$\begin{array}{r} 6590 \\ -1794 \\ \hline 5396 \end{array}$$

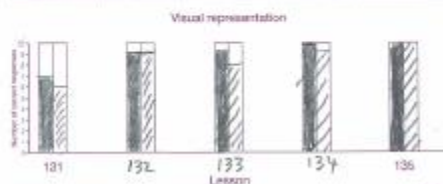
$3 \text{ cm} \times 6 = 18 \text{ cm}^2$

Daily Data: Daily, you record and summarise your own data. For incorrect responses classified as Bugs, you shade the BugKey in the corresponding row on the BugBoard. This allows you and your teacher to monitor your progress.

For each Lesson the whole of my data is represented in 2 columns. The first column represents Question group 1-10. For this group I colour code the KEY. Next I fill in the missing labels. Then I shade the column upwards stopping at the number equal to the number of my correct responses. I repeat the process for Question group 11-20.

DAILY DATA

Date	3-12-12	4-12-12	5-12-12	6-12-12	7-12-12	BugBoard					
Round 27	Lesson 131	Lesson 132	Lesson 133	Lesson 134	Lesson 135	131	132	133	134	135	
Question 1	846648	868842	883004	871088	874684	☉	☉	☉	☉	☉	1
Question 2	4496	2196	6296	8496	5396	☉	☉	☉	☉	☉	2
Question 3	+	-	-	28	(1150)+	☉	☉	☉	☉	☉	3
Question 4	17	9	$4\frac{2}{5}$	$31\frac{1}{2}$	11	☉	☉	☉	☉	☉	4
Question 5	50	15	9	63	29	☉	☉	☉	☉	☉	5
Question 6	-	-	-	+	÷	☉	☉	☉	☉	☉	6
Question 7	2	3	5	4	10	☉	☉	☉	☉	☉	7
Question 8	$\frac{1}{3}$	$\frac{3}{3}$	$\frac{1}{5}$	$\frac{1}{3}$	$\frac{1}{3}$	☉	☉	☉	☉	☉	8
Question 9	12%	14	$\frac{2}{100}$	5%	$\frac{9}{100}$	☉	☉	☉	☉	☉	9
Question 10	200	500mL	1g	201g	2.10g	☉	☉	☉	☉	☉	10
Question 11	6	6	c	a	b	☉	☉	☉	☉	☉	11
Question 12	24cm	54cm ²	6cm ²	12cm ²	13cm ²	☉	☉	☉	☉	☉	12
Question 13	Tail	Head	2	3	1h, 1t	☉	☉	☉	☉	☉	13
Question 14	2	10	3	4	5	☉	☉	☉	☉	☉	14
Question 15	10	12	2	18	12	☉	☉	☉	☉	☉	15
Question 16	3	60sec	1	2min	1.2km	☉	☉	☉	☉	☉	16
Question 17	15	6	30	10	25	☉	☉	☉	☉	☉	17
Question 18	East	North	South	North	SE	☉	☉	☉	☉	☉	18
Question 19	(9, 8)	(8, 6)	Pond	Pond	Bulb	☉	☉	☉	☉	☉	19
Question 20	16	16	12	$\frac{1}{2}$	$\frac{5}{2}$	☉	☉	☉	☉	☉	20
My score	13	18	17	19	20						
Out of	20	20	20	20	20						



Key Questions 1-10 Questions 11-20

After recording and summarising my data, I go to page 98 and complete my task for the Round.

myEMMdata
p 52–53

myJEMM+data
p 38–39

myJEMMdata
p 52–53

ROUND 13 TASK

STEP 1 Look at the Graph titled How Sam scored points Round 13: Questions 1–10. Each space represents one score point. The KEY gives category information about each space. For example, Sam scored 3 for Question 2.

STEP 2 Use the Graph and Record table titled How Sam scored points Round 13: Questions 1–10, to answer these questions:

- How many points did Sam score for Question 5?
- What is the maximum possible Sam can score for Questions 1–10 in one Lesson?
- How many points did he score for Number patterns?
- What is his total score for Round 13 Questions 1–10?
- For which question did he score most points?
- What fraction of the whole represents points he did not score?

END OF TASK

ROUND 14 TASK

STEP 1 In the Record table titled How I scored points Rounds 14 and 15: Questions 1–10, put ticks in each lesson column (66–70) to show how you scored points in Round 14.

STEP 2 Use the Record table to answer these questions:

- How many points did you score for Question 5?
- What is the maximum possible you can score for Questions 1–10 in one Lesson?
- How many points did you score for Number patterns?
- What is your total score for Round 14 Questions 1–10?
- For which question/e did you score most points?
- What fraction of the whole represents points you did not score?

END OF TASK

STEP 1 In the Record table titled How I scored points Rounds 14 and 15: Questions 1–10, put ticks in each lesson column (71–75) to show how you scored points.

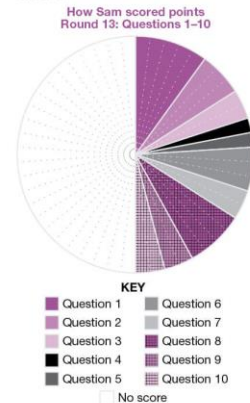
STEP 2 Look at the Graph titled How I scored points Round 15: Questions 1–10. Each space represents one score point. The KEY gives category information about each space. Use a different colour and/or pattern to code

Round Task: EMM is structured into 32 rounds each consisting of 5 lessons. At the end of each round you read, interpret and complete tables and graphs building on the visual representation knowledge you have acquired.

RECORD TABLE

How Sam scored points Round 13: Questions 1–10					
Round	13				
Lesson	61	62	63	64	65
Question 1 Addition	✓	✓	✓	✓	✓
Question 2 Subtraction		✓	✓		✓
Question 3 Multiplication	✓	✓			
Question 4 Division				✓	
Question 5 Number patterns			✓		
Question 6 Equation and inverse operations	✓	✓			✓
Question 7 Whole number properties				✓	✓
Question 8 Fractions		✓	✓	✓	✓
Question 9 Decimals				✓	✓
Question 10 Measurement				✓	✓

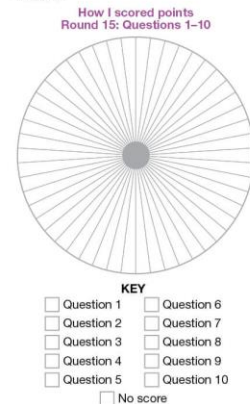
GRAPH



RECORD TABLE

How I scored points Rounds 14 and 15: Questions 1–10										
Round	14					15				
Lesson	66	67	68	69	70	71	72	73	74	75
Question 1 Addition										
Question 2 Subtraction										
Question 3 Multiplication										
Question 4 Division										
Question 5 Number patterns										
Question 6 Equation and inverse operations										
Question 7 Whole number properties										
Question 8 Fractions										
Question 9 Decimals										
Question 10 Measurement										

GRAPH



I enter my data in the table on the facing page then complete the Self-evaluation below.

EMM Student Self-evaluation

Lessons 1 to 20

Name _____ Date ____/____/____

In the last twenty lessons my scores are as follows:

	Score	Out of	
1 Addition		20	From these scores I make the following assessment of my progress: • My EMM strand of strength is _____ because _____ • The EMM strand I most need to improve is _____ • I can improve my overall EMM scores by _____ • The amount of effort I put into these lessons was _____ • At the moment EMM is making me feel _____
2 Subtraction		20	
3 Multiplication		20	
4 Division		20	
5 Number patterns		20	
6 Equations and inverse operations		20	
7 Whole number properties		20	
8 Fractions		20	
9 Decimals		20	
10 Measurement		20	
11 Space		20	
12 Geometry		20	
13 Average, percentage, ratio, chance		20	
14 Math language		20	
15 Money		20	
16 Time		20	
17 Algebra		20	
18 Visual perception		20	
19 Data analysis		20	
20 Problem solving		20	

My teacher's comment:

MY TOTAL SCORE

	Round 1	Round 2	Round 3	Round 4	My score	Out of
Question 1 Addition						20
Question 2 Subtraction						20
Question 3 Multiplication						20
Question 4 Division						20
Question 5 Number patterns						20
Question 6 Equations and inverse operations						20
Question 7 Whole number properties						20
Question 8 Fractions						20
Question 9 Decimals						20
Question 10 Measurement						20
Question 11 Space						20
Question 12 Geometry						20
Question 13 Average, percentage, ratio, chance						20
Question 14 Math language						20
Question 15 Money						20
Question 16 Time						20
Question 17 Algebra						20
Question 18 Visual perception						20
Question 19 Data analysis						20
Question 20 Problem solving						20

myEMMdata
p 12–13

myJEMM+data
p 12–13

myJEMMdata
p 12–13

Self-evaluation: After each group of 20 lessons you self-evaluate and reflect on your growth in knowledge, understanding and achievement.

MMSanimation

Voice-over with animation: animations reflect that critical part of Math Mastery Series lesson script (shown in coloured CAPS) requiring the teacher to point on the electronic display.

Lesson 21

Question 5

9

1 8

2 7

3 6

4 5

Lesson 1

Question 2

$$\begin{array}{r} \text{addend} \\ \hline 7 \\ \hline \end{array} + \begin{array}{r} \text{addend} \\ \hline 3 \\ \hline \end{array} = \begin{array}{r} \text{sum} \\ \hline 10 \\ \hline \end{array}$$

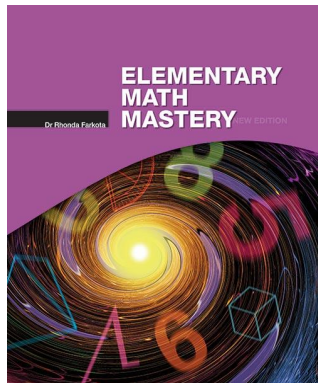
1	2	3	4	5	6	7	8	9	10
10	9	8	7	6	5	4	3	2	1
1	2	3	4	5	6	7	8	9	10

Each program, JEMM, JEMM+ and EMM, comprises:

Teacher Book

Contains presentation lesson scripts with exact instructional wording.

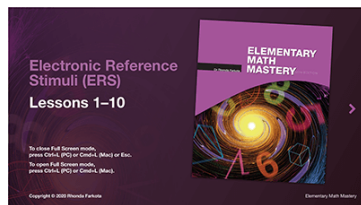
JEMM	80 lessons
JEMM+	120 lessons
EMM	160 lessons



Electronic Reference Stimuli (ERS)

Includes all visual diagrams, formulas and display material (free download provided with the purchase of Teacher Book).

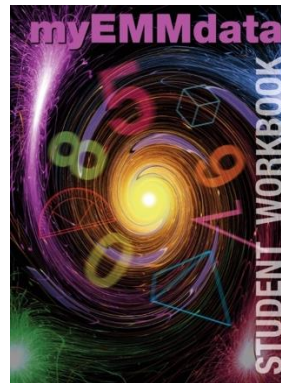
JEMM	680 ERS stims
JEMM+	1800 ERS stims
EMM	3200 ERS stims



Student Workbook

An academic journal where students record, analyse and map performance.

myJEMMdata	92 pages
myJEMM+data	124 pages
myEMMdata	152 pages



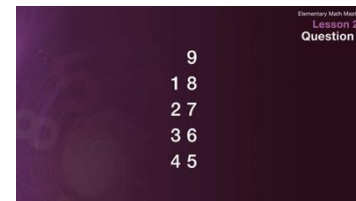
MMSAnimation

JEMManimation
JEMM+animation
EMManimation

Voice-over with animation: the animations reflect that critical part of the Math Mastery Series lesson script (shown in coloured CAPS) requiring the teacher to point on the electronic display.

JEMM	680 videos
JEMM+	1800 videos
EMM	3200 videos

You can access MMSAnimation Lessons 1-10 freely.



Research on Learning

The effectiveness of the Math Mastery Series is dependent on the quality of implementation. Where the quality of implementation is high, and when implemented as prescribed, effective learning is assured.

Teacher Book Introduction and sample lessons: <https://mathmasteryseries.com.au/sample-materials/>

Implementation Plan: <https://mathmasteryseries.com.au/implementation-plan/>

Implementation Checklist: <https://mathmasteryseries.com.au/implementation-checklist/>

Professional Learning Reading Plan:

<https://mathmasteryseries.com.au/professional-learning-reading-plan/>

Resources to assist the teacher in introducing aspects of Student Workbooks:

<https://mathmasteryseries.com.au/student-workbook/>

MMSanimation: mathmasteryseries.com.au/mmsanimation/

and select **EMManimation** or **JEMM+animation** or **JEMManimation**

Dr Rhonda Farkota


Monash University

The effects of DI in the regular math class on student self-efficacy and achievement.

<http://www.acer.org/files/FarkotaThesis.pdf>

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